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## Triple configurations of pursuit shock waves in conditions of ambiguity of the solution

The article studies triple configurations of shock waves in supersonic flows of a perfect gas in view of the fact that it is not always possible to determine unambiguously the parameters of the remaining shocks in the configuration by specifying the properties of the oncoming flow and the branching shock wave. The values of the parameters of triple configurations with maximum relations of the parameters of the flow on the sides of the outgoing tangential discontinuity (extremal configurations) in conditions of the ambiguity of the physically realizable solution are found analytically and numerically.

**Keywords:** triple configurations, shock waves, supersonic flow.

### Introduction

Triple configurations of shock waves, present in stream and nozzle gas flows implemented in jet aviation and rocketry technologies, affect the performance of supersonic air intakes and other equipment based on jet flow technologies.

At the present time, developers keep on searching for effective solutions for ramjet, rotating, and pulse detonation engines, so the problem of analysing interaction between compression shocks, shock and explosive waves is especially relevant. To solve this problem, it is necessary to analyse all triple configurations that may form in given conditions, depending on device parameters. It is also important to analyse a variety of possible solutions to the problems regarding development of explosive-proof equipment, determination of damage effect caused by condensed substance explosion associated with irregular interaction of air shock waves and their Mach reflection.

This paper briefly reviews the properties of optimal triple configurations that correspond to the maximum variations in the parameters of flows after them and are inherent to the basic and alternative solutions within the framework of the local triple shock theory. In this respect, when searching for the optimal flow conditions in triple configurations, we must consider the ambiguity in solution to the constitutive system of equations.

### General information on triple configurations

A triple configuration of compression shocks is a shock-wave structure consisting of three shock waves with a common triple point (point  $T$  in Fig. 1). Triple configurations of shock waves,

being stationary within a selected coordinate system (compression shocks), are present in stream and nozzle gas flows implemented in jet aviation and rocketry technologies [1–3]. They affect the performance of supersonic air intakes and other equipment based on jet flow technologies [4, 5]. Triple configurations of moving (travelling) shock waves appear under their Mach reflection and irregular interaction [6–10], affecting the efficiency of the mechanical impact of an explosion, as well as the performance of explosion-proof devices intended to suppress the high-explosive effect [11–13], in particular, in case of multiple interaction of shock waves in confined volumes [14–16]. Gas flows having passed through different compression shock wave systems (sequence of shocks 1 and 2 or single shock 3) are separated by tangential discontinuity  $\tau$ . The parameters of shocks are connected by the conditions of consistency on tangential discontinuity, written in the form [17–19]:

$$J_1 J_2 = J_3; \quad (1)$$

$$\beta_1 + \beta_2 = \beta_3. \quad (2)$$

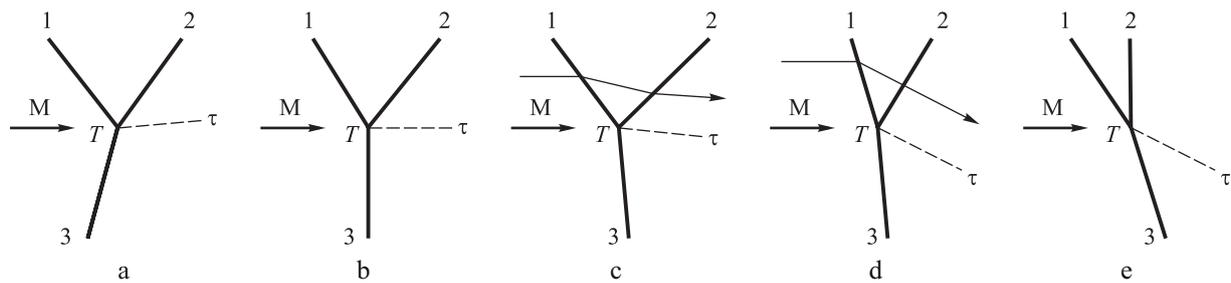
Here,  $J_i (i = 1...3)$  – intensity of the  $i$ -th shock (ratio of static pressures after and before the shock);

$\beta_i$  – flow turn angle on the surface of the  $i$ -th shock.

Angles  $\beta_i$  and Mach numbers  $M_i$  after the  $i$ -th shock are associated with shock intensity and Mach number  $M_k$  before the shock by the known [1] classic relationships.

Depending on the direction of flow turn on shocks 1–3, three types of triple configurations are

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**Fig. 1.** Types of triple configurations:  
a – TC-1; b – TC-2; c – TC-3; d – SMC; e – TTC-2-3

distinguished. In configurations of the first type (TC-1, Fig. 1, a), flow turn on shock 1 occurs in a direction different from that on shocks 2 and 3. For example, at  $\beta_1 < 0$ , angles  $\beta_2 > 0$ ,  $\beta_3 > 0$ . In configurations of the second type (TC-2, Fig. 1, b), the direction of turn on shock 2 is different from the others, and in configurations of the third type (TC-3, Fig. 1, c), flow turn occurs in the same direction on all the shocks. The stationary Mach configuration (SMC, Fig. 1, d) with direct main shock ( $\beta_3 = 0$ ) and configuration TTC-2-3 (Fig. 1, e) with direct shock 2 ( $\beta_2 = 0$ ) are transient.

Setting adiabatic index  $\gamma$ , Mach number  $M$  of flow before the triple point, and branching shock intensity  $J_1$  does not always allow to explicitly define the properties of other shocks in the system of equations (1)–(2). The same parameters  $\gamma$ ,  $M$ , and  $J_1$  are matched by up to three physically based solutions with different values of  $\beta_2$  and  $\beta_3$ . The basic solution to the system of equations (1)–(2) is defined in the widest area of parameter space  $(\gamma, M, J_1)$ , and two alternative solutions – only at subsets of the region of the basic solution definition. Triple configurations corresponding to the basic solution may belong to all three types, as well as to the transient configurations SMC and TTC-2-3. Alternative triple configurations (ATC) relate to the third type (see Fig. 1, c), and the flow after shock 2 is supersonic at that. They are formed as a result of interaction between pursuit shocks.

Many parameters of gas flows after triple configurations have substantial differences. Those of interest are the differences in stagnation pressures  $p_0$ , velocities  $V$ , flow rate functions  $q = \rho V$ , flow strength  $d = \rho V^2$ , flow pulses  $j = p + \rho V^2$  after the triple point. The measure of difference here are their ratios on the tangential

discontinuity sides. Triple configurations with extremal values of such ratios are called optimal configurations. Investigation of the optimal configurations may have practical importance in analysing the origin of self-oscillation regimes of flows in free and impact supersonic jets [20], when designing the equipment generating pulsating gas flows.

Further, we shall analyse the properties of optimal triple configurations corresponding to both the basic and alternative solutions. The numerical results are given for  $\gamma = 1,4$ .

**Optimal configurations corresponding to the basic solution**

The properties of triple configurations of compression shock waves are analysed on the plane of parameters  $M$  and  $\sigma_1$  (Fig. 2), where  $\sigma_1$  – angle of shock 1 to the direction of flow before the shock. Angle  $\sigma_1$  correlates with shock intensity  $J_1$  as

$$J_1 = (1 + \varepsilon) M^2 \sin^2 \sigma_1 - \varepsilon,$$

where  $\varepsilon = (\gamma - 1) / (\gamma + 1)$ .

The range of angles  $\sigma_1$  variation is limited from below by curve 1, which corresponds to shock transformation into a weak discontinuity ( $\sigma_1 = \alpha(M) = \arcsin(1/M)$ ,  $J_1 = 1$ ). The values  $\sigma_1$  are limited from above as well, at least by the requirement that shock 2 must exist in the supersonic flow after the branching shock. This requirement is conformed to by the region under curve 2, which is plotted proceeding from condition  $M_1 = 1$  after shock 1.

For the existence of triple configuration, presence of a supersonic flow after shock 1 is insufficient. A solution to the system (1)–(2) exists only in the region between curves 1 и  $f_1$  therefore curve  $f_1$  is the exact upper boundary

of the region under consideration and is defined by the equation common for curves  $f_i (i = 1, 2)$ :

$$M = \left\{ \left[ (1 - 2\varepsilon - \varepsilon^2)J_1^2 + (1 - 5\varepsilon^2)J_1 + 2\varepsilon \times \right. \right. \\ \left. \left. \times (1 - 2\varepsilon^2) \mp 2(1 + \varepsilon J_1) \sqrt{\varepsilon(1 + \varepsilon J_1)(J_1 + \varepsilon)} \right] / (3) \right. \\ \left. / \left[ (1 + \varepsilon)((1 - 3\varepsilon)J_1 - 4\varepsilon^2) \right] \right\}^{1/2}.$$

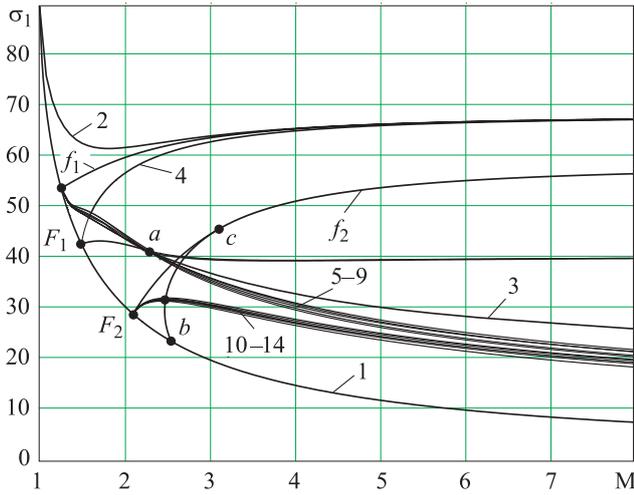


Fig. 2. Parameters of triple configurations

Curve  $f_1$  starts in point  $F_1$  on curve 1, where  $M_{F_1} = 1.245$ ,  $M_{F_2} = 2.54$ .

Solutions to the system (1)–(2) in the region under consideration may correspond to configurations of different types. In the subregion between curves 1 and 3, configurations of TC-1 type are implemented; between curves 3 and 4 – TC-2, and between curves 4 and  $f_1$  – TC-3. Curve 3 corresponds to the stationary Mach configuration and is plotted from solution to the equation

$$aJ_m^2 + bJ_m + c = 0,$$

where  $a = (1 - \varepsilon)(1 + \varepsilon J_1)$ ;

$J_m$  – intensity of direct shock, formed in the flow with a given Mach number,

$$J_m = (1 + \varepsilon)M^2 - \varepsilon;$$

$$b = -\left[ (1 + \varepsilon - \varepsilon^2 + \varepsilon^3)J_1^2 + \varepsilon(1 + \varepsilon)J_1 + (1 - \varepsilon) \right];$$

$$c = J_1 \left[ (1 - \varepsilon^2)J_1^2 - (1 + \varepsilon^2)J_1 - 2\varepsilon \right].$$

Transient configurations TTC-2-3 (curve 4) are determined analytically as well [18, 19].

Intensities and other parameters of compression shock waves across the entire region

of basic solution existence are changing continuously. The parameters of individual shocks take extremal and specific values (e.g., shocks 2 and 3 may correspond to the maximum deviation points, Crocco points, constant pressure points, and sonic point [19]).

The properties of flows after the triple configuration are determined from the system (1)–(2) and ratios on the compression shocks. For example, the ratios between total pressures  $p_0$ , velocities  $V$ , flow rate functions  $q$ , flow strengths  $d$ , flow pulses  $j$  at tangential discontinuity are as follows:

$$I_{p_0} \equiv \frac{p_{02}}{p_{03}} = \left( \frac{E_3}{E_1 E_2} \right)^{\frac{1+\varepsilon}{2\varepsilon}}, \quad I_V = \frac{M_2}{M_3} \sqrt{\frac{E_1 E_2}{E_3}},$$

$$I_q = \frac{M_2}{M_3} \sqrt{\frac{E_3}{E_1 E_2}}, \quad I_d = \frac{M_2^2}{M_3^2}, \quad I_j = \frac{1 + \gamma M_2^2}{1 + \gamma M_3^2}, \quad (4)$$

where  $E_i = \frac{(1 + \varepsilon J_i)}{(J_i + \varepsilon)}$  – inverse ratio of densities on the shock.

The lower boundary of the region of solution existence (curve 1) corresponds to transformation of shock 1 and the upper boundary (curve  $f_1$ ), of shock 2 – into a weak discontinuity. In these cases, all the considered parameter ratios after the triple point are equal to unity. At fixed Mach number  $M$ , the only extremum point of the considered functions in a range between the definition region boundaries is the maximum point. The configurations corresponding to these maxima are optimal at fixed Mach number.

The parameters of configurations optimal with respect to the target functions (4) are shown in Fig. 2 by curves 5–9, respectively. At low Mach numbers, these configurations belong to the third type. The intersections of curves 5–9 with curve 4 corresponds to the optimal transient configurations. In this case, the optimal ratios of parameters ( $I_{p_0} = 1.076$ ;  $I_V = 1.085$ ;  $I_q = 1.107$ ;  $I_d = 1.201$ ;  $I_j = 1.090$ ) are low, and the ratios of Mach numbers ( $M = 1.596$ ;  $M = 1.567$ ;  $M = 1.571$ ;  $M = 1.569$ ;  $M = 1.584$ ) are very close.

With an increase of Mach numbers, the optimal curves 5–9 come close and intersect in one point  $a$ , which corresponds to the stationary Mach



configuration (SMC) with Mach number  $M = \frac{\sqrt{4 - 3\varepsilon + \varepsilon^2}}{(1 - \varepsilon)} = 2.254$ . The intensities of

incident shock 1 and reflected shock 2 of the compression shock waves in such SMC are equal to:  $J_1 = J_2 = \frac{2}{(1 - \varepsilon)} = 2.4$ . It is proved [21, 22] that

equality of the shock wave intensities leads to the total pressure maximum after the shock-wave system if the product of those intensities is a fixed value. It can be shown that in the SMC such a product ( $J_3$  intensity), even though it is not a fixed value, obeys the above theorem, therefore it is exactly the Mach configuration with equal shock intensities that is the optimal one. The parameter ratios after the optimal SMC:

$$I_{p_0} = 1.448, I_V = 1.649, I_q = 1.833, I_d = 3.024, \\ I_j = 1.587.$$

At greater Mach numbers, configurations of the first type are optimal. The optimal values of target functions increase monotonically but in a limited way, while the optimal intensities of shocks 1 and 3 at  $M \rightarrow \infty$  tend to infinity. The configurations optimal in terms of  $I_{p_0}$  have the following finite limits:

$$\frac{J_3}{M^2} \rightarrow C_1, \frac{J_1}{M} \rightarrow \sqrt{C_1}, \frac{J_2}{M} \rightarrow \sqrt{C_1},$$

where  $C_1 = \frac{(1 + \varepsilon - \sqrt{(1 - \varepsilon)^2 + 4\varepsilon^3})}{[2\varepsilon(1 - \varepsilon)]}$ .

The Mach number after shock 1 tends to the infinite limit (order  $\sqrt{M}$ ) and after shocks 2 and 3 – to finite limits. Ratio  $I_{p_0}$  itself tends to the value

$$I_{p_0} \rightarrow \varepsilon^{-(1+\varepsilon)/2\varepsilon} = 529.1. \quad (5)$$

The limit values of other functions in configurations optimal in terms of  $I_{p_0}$ , are as follows:

$$I_V \rightarrow \sqrt{\frac{1 - \varepsilon + \varepsilon^2 + \sqrt{(1 - \varepsilon)^2 + 4\varepsilon^3}}{2\varepsilon^2}} = 4.007,$$

$$I_d \rightarrow \frac{1 - \varepsilon + \varepsilon^2 + \sqrt{(1 - \varepsilon)^2 + 4\varepsilon^3}}{2\varepsilon^3} = 152,$$

$$I_q \rightarrow \frac{1 - \varepsilon + \sqrt{(1 - \varepsilon)^2 + 4\varepsilon^3}}{2\varepsilon^2} = 30.2,$$

$$I_j \rightarrow \frac{1 - \varepsilon + \sqrt{(1 - \varepsilon)^2 + 4\varepsilon^3}}{2\varepsilon^2} = 30.2$$

and, as a rule, they are close to the optimal values reached on curves 6–9 (see Fig. 2):  $I_V \rightarrow 5.261$ ,  $I_d \rightarrow 155.8$ ,  $I_q \rightarrow 30.41$ ,  $I_j \rightarrow 30.22$ ; therefore, optimisation of configurations with respect to these parameters is sometimes substituted for optimisation as per  $I_{p_0}$  [18]. In configurations optimal with respect to these four parameters, intensity  $J_1$  has order  $M^2$ , and values  $M_1$  and  $J_2$  tend to high finite values. The angle of shock 1 tends to a low finite value at that, rather than to zero.

The optimal values (especially, the total pressure ratios) tend to their limits slowly: at  $M = 8$ , optimal  $I_{p_0} = 19.36$ , and at  $M = 200$ ,  $I_{p_0} = 439.2$ . The optimisation of configurations leads to notable increase of the target functions. Thus, at  $M \rightarrow \infty$ , optimal  $I_{p_0} \rightarrow 529.1$ , while  $I_{p_0} \rightarrow 69.72$  in the SMC and  $I_{p_0} \rightarrow 1$  in TTC-2-3.

### Alternative triple configurations

Starting from certain Mach number ( $M = 2.542$  in optimisation as per the ratio of total pressures), parameters ( $M, \sigma_1$ ) of the optimal basic configurations determine two more solutions, and at  $M > 2.61$  – one solution that describes ATC of the third type corresponding to one of the alternative solutions, which exist along with the basic one at the same Mach numbers of the intensity flow of shock 1 (branching) and gas adiabat.

The alternative solutions to the system (1)–(2) appear on curve  $bc$  (see Fig. 2) as a result of decomposition of shock isomachs [13]. There are two different ATCs in curvilinear triangle  $F_2cb$ . One of the solutions in segment  $F_2c$  of curve  $f_2$  corresponds to value  $J_1 < 1$ , due to which it stops being implemented. At the same time, a new and the only possible solution for ATC appears on curve  $f_2$ , after point  $c$ . Curve  $f_2$  and point  $F_2$  are defined by relationship (3), and points  $b$



( $M_b = 2.089$ ) and  $c$  ( $M_c = 3.117$ ) – by high-degree (for point  $b$  – eighth) algebraic equations.

The maxima of equations (4) can be achieved in the ATCs corresponding to the solution which is continuous across the entire region beyond curves  $bc$  and  $f_2$  (curves 10–14). At  $M \rightarrow \infty$ , the optimal value of  $I_{p_0}$  tends to the limit (5) and can be achieved at  $J_3/M^2 \rightarrow C_1$ ,  $J_1/M \rightarrow \sqrt{C_1}$ ,  $J_2/M \rightarrow \sqrt{C_1}$ . The flow turn angle on shock 3 in an optimal asymptotic ATC is opposite to its value in the “basic” configuration.

The limits of other parameter ratios in the optimal ATCs are at least comparable to the “basic” configurations: in the ATC, at  $M = 199.3$ , maximal  $I_v = 4.858$ ,  $I_d = 133.1$ ,  $I_q = 27.47$ ,  $I_j = 28$ , and in the “basic” configurations,  $I_v = 5.257$ ,  $I_d = 151$ ,  $I_q = 29.23$ ,  $I_j = 28.56$ . The relative position (from bottom to top) of the optimal curves 10–14 is opposite to the position of curves 5–9 at high Mach numbers.

With parameter  $\gamma$  increased, Mach numbers at which the ATCs are formed increase substantially and tend to infinity at  $\gamma \rightarrow 5/3$ . At  $\gamma \geq 5/3$ , the system of equations (1)–(2) has no more than one physically based solution.

### Conclusion

The conducted calculation and parametric analysis of triple configurations forming under all theoretically feasible flow parameters before them serve for optimisation of systems and devices that employ the effects of interaction and reflection of compression shock waves, blast shock waves, and detonation waves.

The study demonstrates that triple configurations corresponding to different physically feasible solutions can be optimal: after such configurations, the maximum and quite high ratios of total pressures, velocities, flow strengths, and other flow parameters can be achieved on different sides of tangential discontinuity originating from the triple point. This statement holds true both for the basic (traditionally considered) and additional (alternative) solutions defining triple configurations, therefore, when searching for the optimal flow conditions in triple configurations, it is necessary to consider the ambiguity of solution to the defining system of equations.

The results obtained using theoretical and numerical methods can be used in various applications of gas dynamics. For instance, high total differential pressures in a supersonic gas jet initiate self-oscillation regimes when a jet interacts with obstacles, and lead to extreme acoustic and force loads when executing starting tasks. The different translational (transferred) impact of blast shock waves on bodies located above and below the triple point is achieved due to a considerable difference between flow strengths on the opposite sides of tangential discontinuity. This phenomenon can be used in design of explosion-proof devices and in an analysis of blast effect (especially in confined spaces with inevitable multiple reflection of shock waves and their irregular interaction). Moreover, high values of flow parameters after triple configurations hamper initiation of detonation in aircraft and rocket engines of appropriate type and shall be eliminated at the development phase of such devices.

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### **Тройные конфигурации догоняющих скачков уплотнения в условиях неоднозначности решения**

Рассмотрены тройные конфигурации скачков уплотнения в сверхзвуковых потоках совершенного невязкого газа с учетом того, что с помощью задания свойств набегающего потока и ветвящегося скачка уплотнения не всегда однозначно можно определить параметры остальных скачков конфигурации. Аналитически и численно найдены значения параметров тройных конфигураций с максимальными отношениями параметров течения на сторонах исходящего тангенциального разрыва (экстремальных конфигураций) в условиях неоднозначности физически реализуемого решения.

*Ключевые слова:* тройные конфигурации, скачки уплотнения, сверхзвуковой поток.

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Область интересов: газовая динамика, ударные и взрывные волны, взаимодействие газодинамических разрывов, взрывозащита.

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